

Crime and Punishment.

Experimental Evidence on the Inspection Game.

*Rational Choice Sociology: Theory and Empirical Applications.
Venice International University, 6th December 2006*

Research Question

Theoretical analysis

Experimental Design

Empirical Results

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Research Question

**“Sentence severity and crime: Accepting the null hypothesis.”
(Doob & Webster, 2003)**

**“Penalty has no impact on crime”
(Tsebelis, 1990)**

- 1. How is this puzzle solvable?**
In other words: What is the theoretical argument?
- 2. How is it possible to test the argument**
 - (a) with high construct validity
 - (b) with high internal validity?

Economic model of crime (Becker, 1968)

Decision theoretic formulation

- Criminals as rational actors
- **Higher punishment** → **less crime**

Game theoretic model of crime: Inspection Game

(Tsebelis, 1989, 1990, 1993, 1995)

Criminal	Controller	
	control	not control
crime	$-\pi_1, \pi_2$	$\pi_4, 0$
no crime	$0, -\pi_3$	$0, 0$

- Only mixed equilibria
- *Criminals'* decision based on *controller's* utility → **punishment no impact on crime**
- *Controller's* decision based on *criminal's* utility → **punishment impact on control**
- **Conclusion:** Interaction between criminals and controllers neglected so far

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Review: Inspection Game (Tsebelis, 1989)

Criminal	Controller	
	control	not control
crime	$-\pi_1, \pi_2$	$\pi_4, 0$
no crime	$0, -\pi_3$	$0, 0$

Extension: Welfare loss due to crime has to be incorporated in model because

- (a) Theoretical model reflects better what we mean by crime
- (b) Higher construct validity in experiment

However: Conclusions might be different

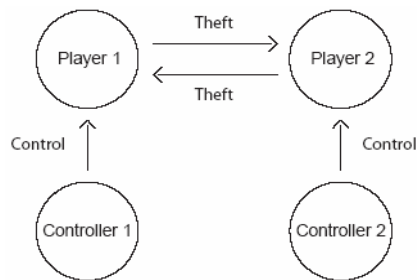
Extended inspection game:

2 "players" who can commit crime. Crime defined as welfare transfer, which

- (a) increases player's payoff on cost of other player's payoff
- (b) decreases collective welfare

1 controller for each "player" with:

- (a) negative control costs
- (b) positive net rewards for successful controls



Player:

- s:= Welfare transfer
- γ := Welfare inefficiency; $0 < \gamma < 1$
- p:= Punishment; $\gamma s < p$

Controller:

- k:= control cost
- r:= reward; $r > k$

Theoretical analysis

Payoffs

$$u \begin{pmatrix} P1 \\ P2 \\ C1 \\ C2 \end{pmatrix} (s_1, s_2, c_1, c_2) = \begin{pmatrix} s_1(\gamma s - c_1 p) - s_2 s \\ s_2(\gamma s - c_2 p) - s_1 s \\ c_1(s_1 r - k) \\ c_2(s_2 r - k) \end{pmatrix}$$

Best answers

$$s_1^R = \begin{cases} 1 & , \gamma s > c_1 p \\ [0, 1] & , \gamma s = c_1 p \\ 0 & , \gamma s < c_1 p \end{cases}, \quad s_2 = \begin{cases} 1 & , \gamma s > c_2 p \\ [0, 1] & , \gamma s = c_2 p \\ 0 & , \gamma s < c_2 p \end{cases}$$

$$c_1 = \begin{cases} 1 & , s_1 r > k \\ [0, 1] & , s_1 r = k \\ 0 & , s_1 r < k \end{cases}, \quad c_2 = \begin{cases} 1 & , s_2 r > k \\ [0, 1] & , s_2 r = k \\ 0 & , s_2 r < k \end{cases}$$

Pure Nash equilibria

$$c_1 = 1 \Rightarrow s_1 = 0 \Rightarrow c_1 = 0 \Rightarrow s_1 = 1 \Rightarrow c_1 = 1 \Rightarrow s_1 = 0$$

Result: No pure equilibria

Mixed Nash equilibrium:

$$s_1^* = s_2^* = \frac{k}{r}$$

$$c_1^* = c_2^* = \frac{\gamma s}{p}$$

In Words:

Probability of crime: Control costs / Reward

Probability of control: Loot / punishment

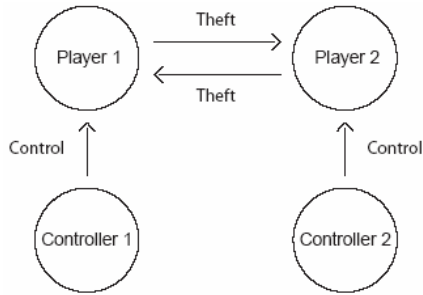
Research Question

Theoretical analysis

Experimental Design

Empirical Results

Experimental Design

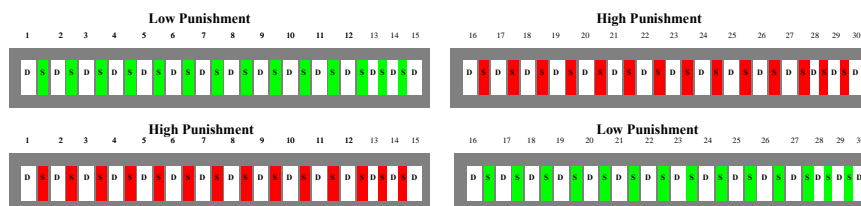


- ↳ Subjects earn money in knowledge quiz
- ↳ Subjects randomly split half into »players« and »controllers«
- ↳ Each player randomly matched with one different player and controller each period
- ↳ Players can take simultaneously money from personal account of the other
- ↳ Controllers could invest control costs to reveal decision of matched player.
- ↳ Conducted with Z-tree (Fischbacher) in computer lab

Experimental Design

2 Experiments:

- 1) Low punishment → High punishment (5 sessions à 20 subjects, 48 players, 48 controllers)
- 2) High punishment → Low punishment (5 sessions à 20 subjects, 50 players, 50 controllers)



Experimental Design

Parameters and information conditions

Players		Low Punishment	High Punishment
s_1	Loss victim	10	10
γ	crime inefficiency parameter	0.5	0.5
γs_2	Gain thief	5	5
p_c	Strength of punishment	6	25
Exchange Rate (Pt.- €)		0.1	0.1
Controllers			
k_c	Control costs	5	5
r_c	Reward succesful control	10	10
Exchange rate (Pt.- €)		0.02	0.02

Experimental Design

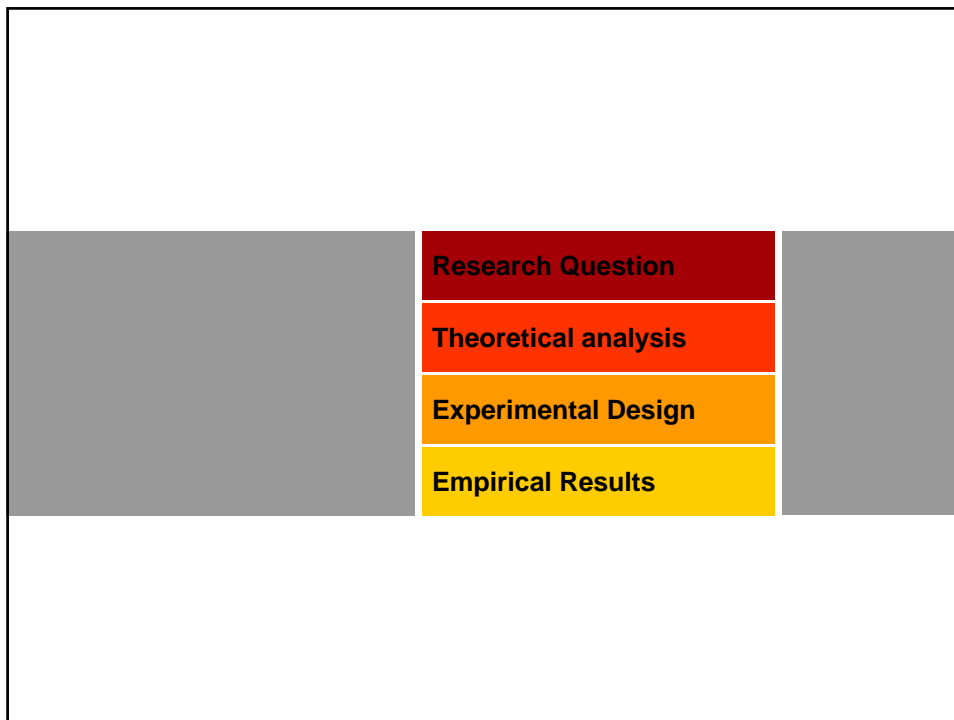
Predictions

$$s_1^* = s_2^* = \frac{k}{r} \quad \frac{k}{r} = \frac{5}{10} = 0.5$$

$$c_1^* = c_2^* = \frac{\gamma s}{p} \quad \frac{\gamma s}{p} = \frac{5}{6} = 0.8 \quad \frac{\gamma s}{p} = \frac{5}{25} = 0.2$$

Prediction 1: Theft rate → 0.5 all 30 periods

Prediction 2: Control rate → 0.8 low punishment condition
→ 0.2 high punishment condition



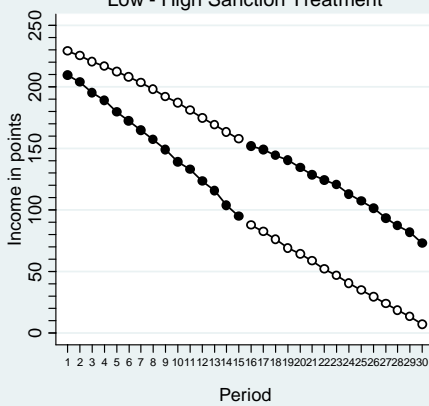
	Empirical Results	
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Subjects

- ↳ 5 Euro show up fee + 5 Euro stakes in average
- ↳ 196 subjects
- ↳ Randomly chosen from address pool of 692 students from various fields from the University of Leipzig
- ↳ Randomly allocated to one experimental session

(1) Description of welfare dynamic over time

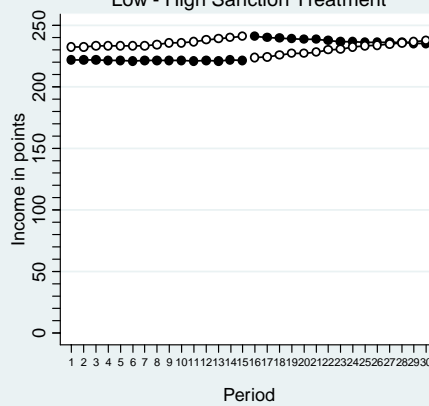
Income change for players
Low - High Sanction Treatment



○ Low Punishment (Net Punishment = 1 Pt.)
● High Punishment (Net Punishment = 20 Pts.)

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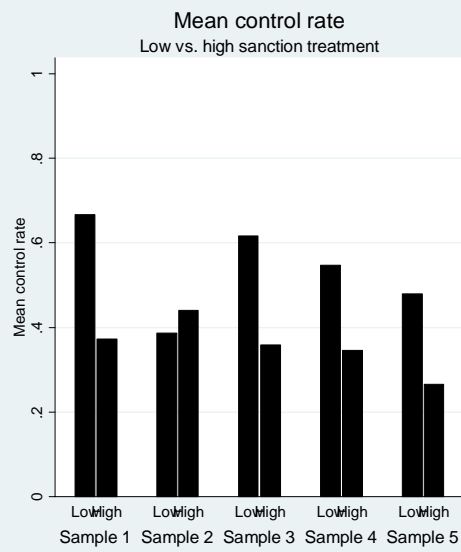
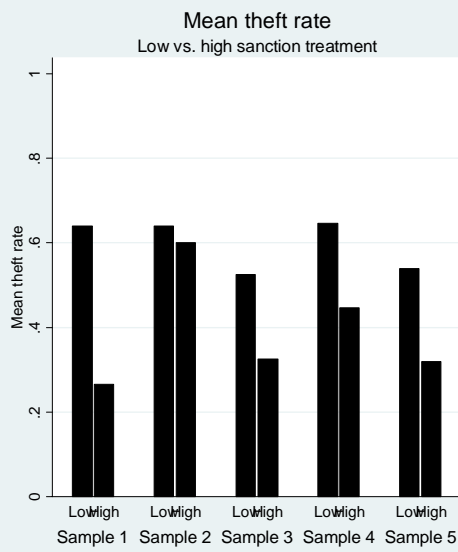
Income change for controllers
Low - High Sanction Treatment



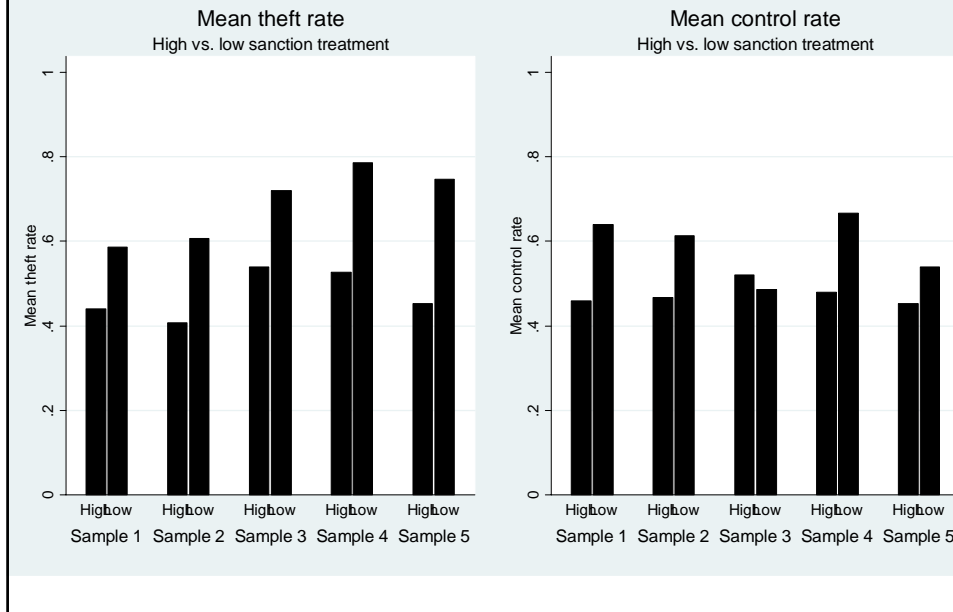
○ Low Punishment (Net Punishment = 1 Pt.)
● High Punishment (Net Punishment = 20 Pts.)

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(2) Static analysis of mixing



Empirical Results



Empirical Results

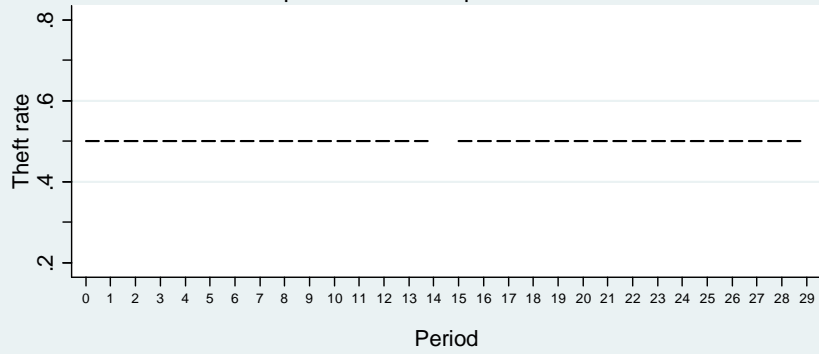
(3) Dynamic analysis of mixing:

Learning dynamic results in convergence towards Nash equilibria

(Macy, 1991; Roth & Erev, 1995; Fudenberg & Levine, 1998; Macy & Flache, 2002)

Empirical Results

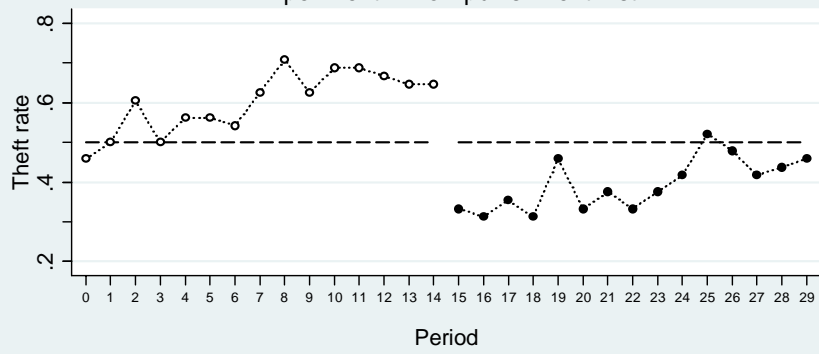
Theft for low and high punishment
Experiment 1: Low punishment first



Low Punishment (Net Punishment = 1 Pt.)	High Punishment (Net Punishment = 20 Pts.)
----- Theoretical prediction	----- Theoretical prediction
Observed values	Observed values
Regression prediction	Regression prediction

Empirical Results

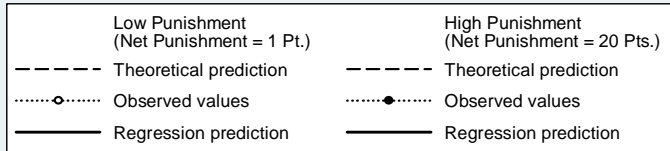
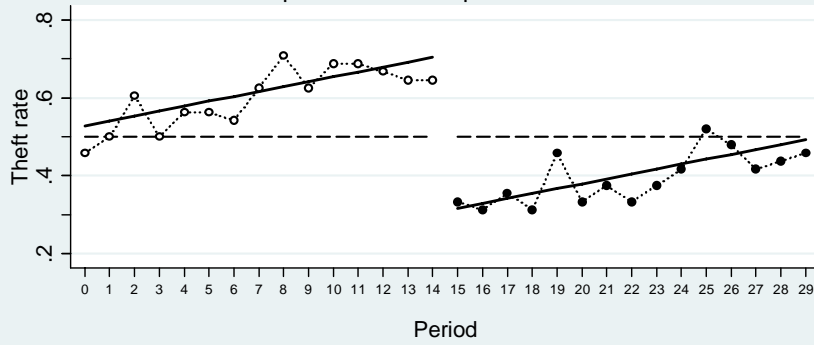
Theft for low and high punishment
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----- Theoretical prediction	----- Theoretical prediction
.....○..... Observed values●..... Observed values
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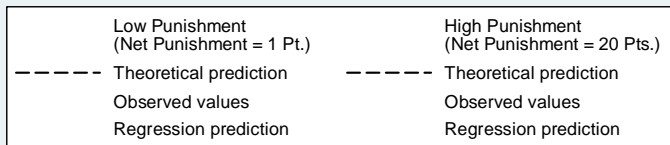
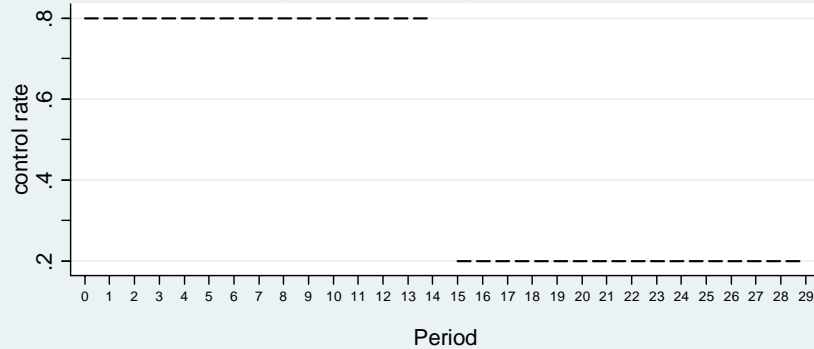
Empirical Results

Theft for low and high punishment
Experiment 1: Low punishment first



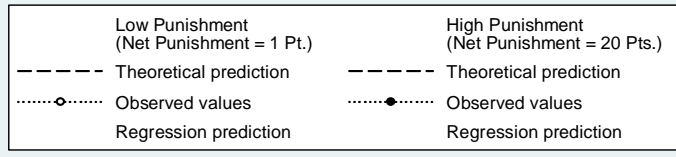
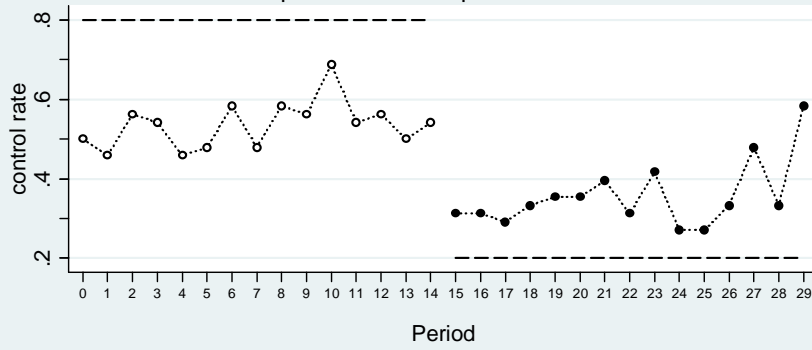
Empirical Results

Control for low and high punishment
Experiment 1: Low punishment first



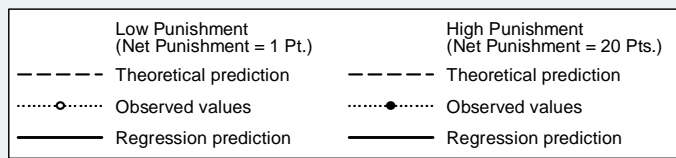
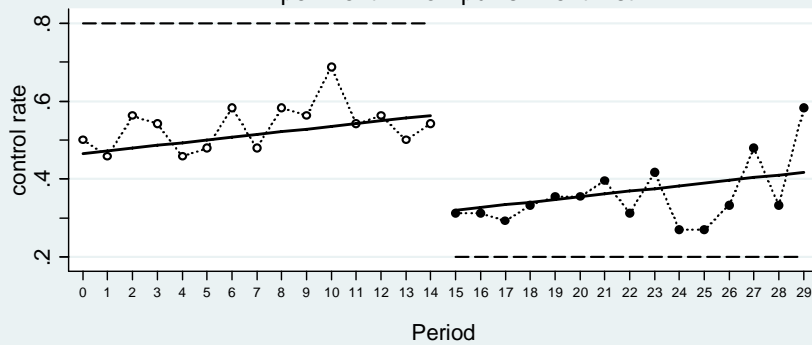
Empirical Results

Control for low and high punishment
Experiment 1: Low punishment first



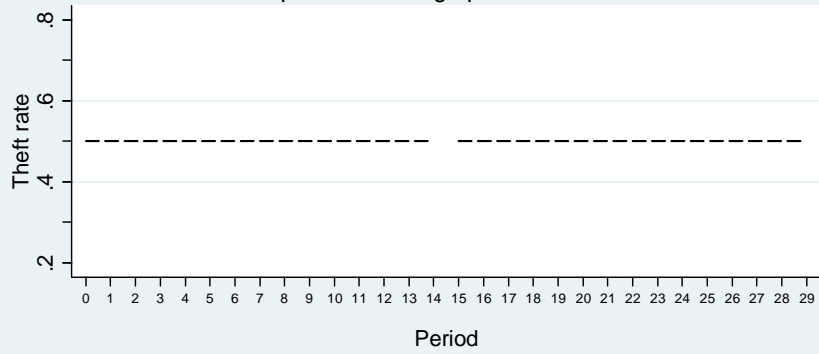
Empirical Results

Control for low and high punishment
Experiment 1: Low punishment first



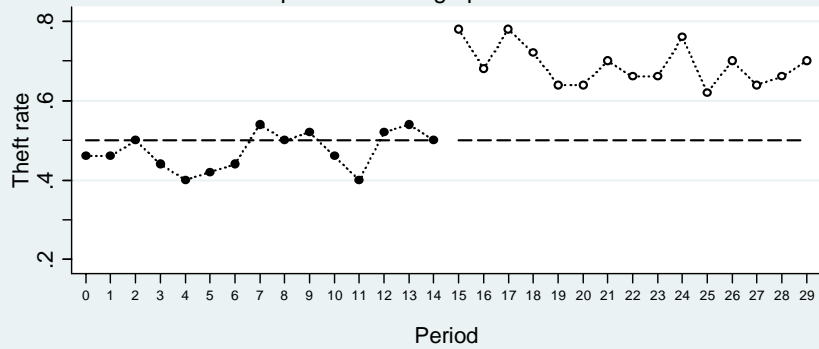
Empirical Results

Theft for low and high punishment
Experiment 2: High punishment first



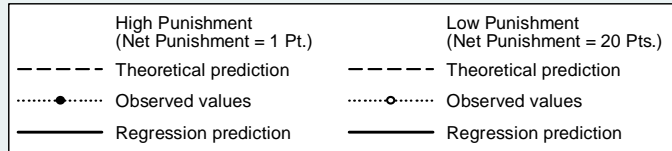
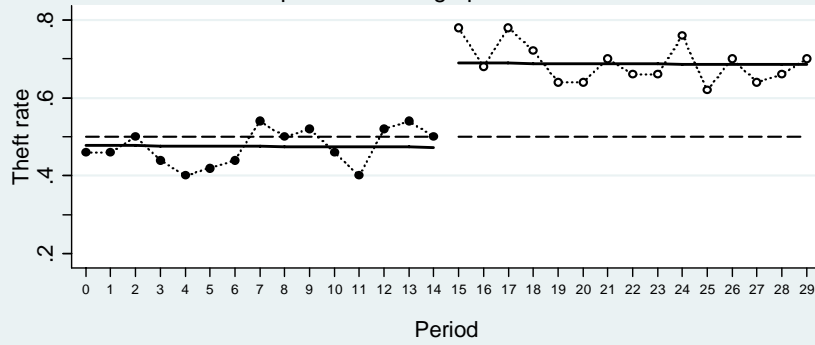
Empirical Results

Theft for low and high punishment
Experiment 2: High punishment first



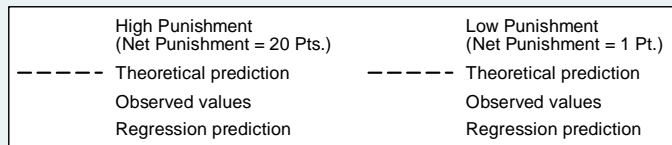
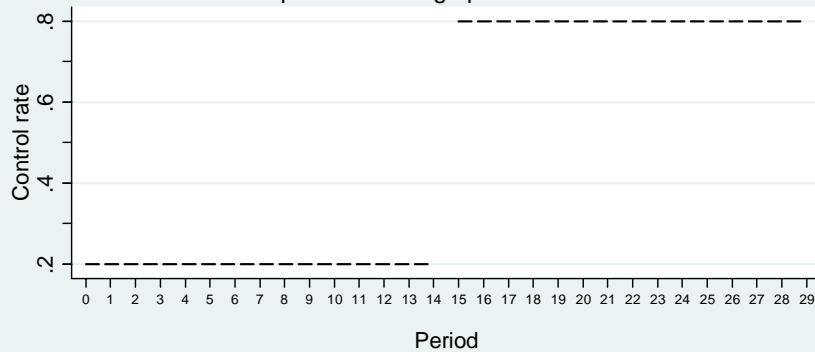
Empirical Results

Theft for low and high punishment
Experiment 2: High punishment first



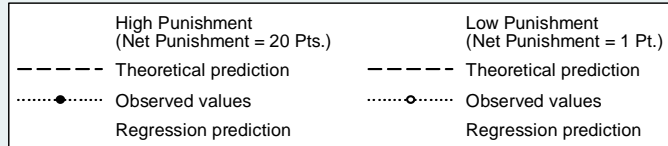
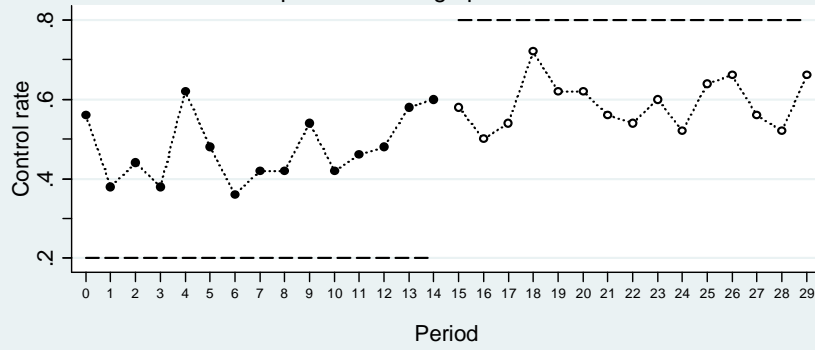
Empirical Results

Control for low and high punishment
Experiment 2: High punishment first



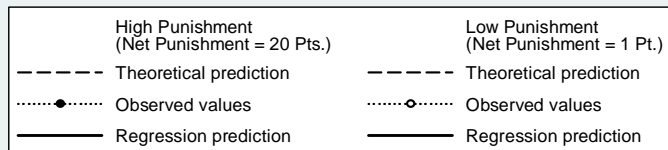
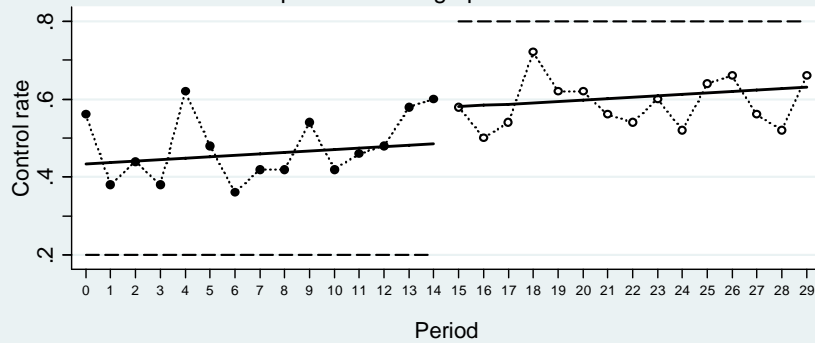
Empirical Results

Control for low and high punishment
Experiment 2: High punishment first



Empirical Results

Control for low and high punishment
Experiment 2: High punishment first



		Empirical Results		
Regression Models for Theft and Control	Model	(1) Theft	(2) Control	
	Linear Random intercept & random Period models	Intercept	0.69 * <i>(22.18)</i>	0.58 * <i>(19.14)</i>
	Error Covariance Structure: Compound Symmetry	High Punishment	- 0.21 * <i>(- 12.53)</i>	- 0.15 * <i>(- 8.36)</i>
		First low punishment	- 0.16 * <i>(- 4.99)</i>	- 0.11 * <i>(- 3.44)</i>
		Period / 15 (First low punishment)	0.19 * <i>(4.50)</i>	0.10 * <i>(2.40)</i>
	Period / 15 (First high punishment)	- 0.00 <i>(- 0.12)</i>	0.05 <i>(1.27)</i>	
	Random intercept	0.0183	0.0142	
	Random period	0.0005	0.0004	
	* significant at 5%, t-values in parentheses			

		Empirical Results	
Conclusions			
1.	Higher punishment	→	less control
2.	Higher punishment	→	less crime
3.	Controllers insensitive:	Control too little for low punishment and too much for high punishment	
4.	Criminals sensitive:	Adapt to inefficiency of controllers	
5.	Efficient policy:	High control incentives	

Next steps:

1. Do higher control incentives result in less crime?

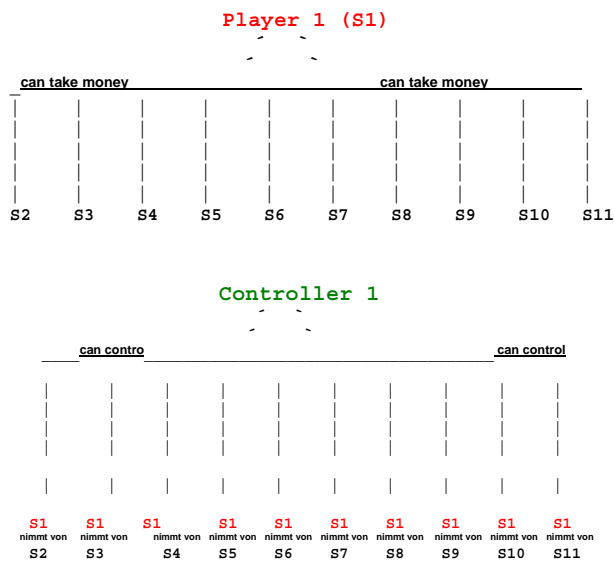
→ 2nd Experiment on variation of reward levels

2. Improvement of measurement

- (a) Metric measurement of crime & control: "Frequentistic" design
- (b) More periods

→ 3rd Experiment

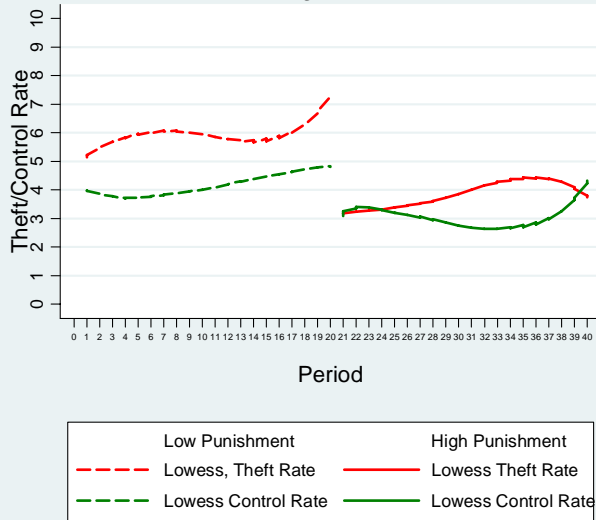
Pilotstudy: Frequentistic Inspection Game



Empirical Results

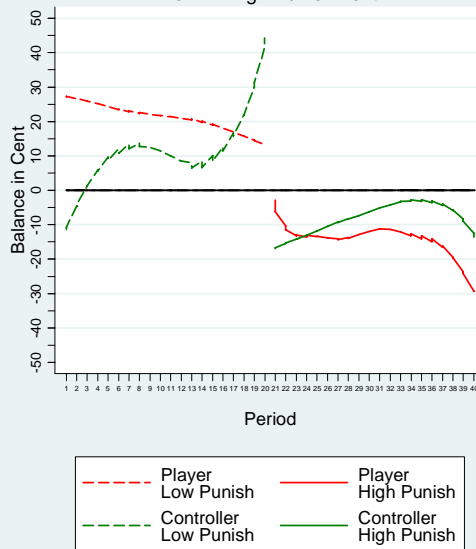
Pilotstudy (n=44)

Frequentistic Inspection Game
Low -> High Punishment



Pilotstudy (n=44)

Balance players vs. controllers
Low -> High Punishment



Preliminary Conclusion for frequentistic design

1. *Frequentistic design allows for more precise testing of mixing hypotheses*
2. *Low punishment results in positive “balance” while high punishment results in negative “balance” for both parties*