Hartmut Esser (University of Mannheim) Julian Seuring (Lifbi Bamberg)

#### What is Your Replicandum?

On the importance of an explicit theoretical foundation of the definition of estimands, especially in replications, using the example of the debate on Ability-Tracking

Seminar "Analytical Sociology: Theory and Empirical Applications" Venice14 <sup>th</sup>. November 2022 Hartmut Esser (University of Mannheim) Julian Seuring (Lifbi Bamberg)

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Seminar "Analytical Sociology: Theory and Empirical Applications" Venice14 <sup>th</sup>. November 2022 Estimands and Replicands The Dispute Theory Re-Corrections Conclusions

#### **Estimands and Replicands**

The Dispute Theory Re-Corrections Conclusions



## Lundberg et al. 2020

lan Lundberg

W

November 1, 2020

Repecca Joinson

We make only **one point** in this article. Every quantitative study must be able to answ

#### estin Mind your estimand ...

questions. the link be

(1) set a **theoretical estimand**, clearly connecting this quantity to theory, (2) link to an empirical estimand, which is informative about the theoretical estimand under some identification assumptions,

# Auspurg&Brüderl 2022

... that the social sciences are not rigorous enough to provide definitive answers. ... We argue that the main **Original Ar** Has th reason was an **unclear** research question. Been C the "M

## ... especially in replications

Abstract In 2018, Silberza question with th skin tone? The that the social results diverged interpretation o show by reanaly theory-guided ca social science re

The broad conclusion of our reanalysis is that social science research needs to be more precise in its "estimands" to become credible.

#### Keywords

Pro

Katr

credibility crisis, cro sensitivity analysis, estimands

#### A first conclusion

Replications are absolutely **necessary**, but are **no** warranty for ,,truth-(approximation)"

Problem 1: Stable repetition of the same mistakes.Problem 2: False refutation of a correct model.

### Main point:

Valid analyses and replications **presuppose** a well-founded and explicit **theory/causal model**, which **defines** the theoretical and empirical estimands, and **any** change against the original study has to be justified by a well-founded and explicit **theoretical** argument.

#### Main aim:

Demonstrating how important **careful** attention to **theoretical** guidelines can be in making correct or false decisions in the research process, but especially in replications.

#### **Topic: Effects of Ability-Tracking**

**general**: Is "Ability"-Tracking theoretically **equivalent** to "Achievement"-Tracking? **specific**: Simultanuous **control** of Abilities and Achievement allowed?

Estimands and Replicands The Dispute Theory Re-Corrections Conclusions

#### **Two Positions**

#### **Differentiation-Position**

Sörensen 1970 Sörensen&Hallinan 1974

Cognitive **homogeneity** of school classes allows better adaptation of **curriculum and instruction** – **achievement** higher **without** increasing social inequality.

**Integration-Position** 

Oakes 1985 Gamoran 2009

Support by **peer-interactions** possible only with **heterogeneity** of school classes (with late or no sorting at all) – **achievement** higher **without** increasing social inequality.

#### **Differentiation-Position**

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Cognitive **homogeneity** of school classes allows better adaptation of curriculum and instruction: achievement higher (without increasing social inequality).

#### **Integration-Position**

Oakes 1985 Gamoran 2009

Support by peer-interactions possible only with **heterogeneity** of school classes (with late or no sorting at all): achievement higher (with decreasing social inequality).

" ... where **tracking** systems are present, **achievement** tends to **diverge**, and to **reinforce** initial differences by **social class**."

#### Gamoran 2009: 9

#### **Empirical Findings**

really?

... in its **empirical** approach **far away** from the respective **theoretical** foundations! Wößmann et al. 2009 Müller&Kogan 2010 van de Werfhorst &Mijs 2010 Müller&Kogan 2010 Becker&Solga 2012 Strello et al. 2019 Terrin&Triventi 2022

...

The actual case



... extension and completion of Sörensen&Hallinan (1970, 1977, 1994)







... extension and completion of Sörensen&Hallinan (1970, 197, 1994)



#### **Rejoinders & Replications**

Klemm 2021 Matthewes&Heisig 2022 Lorenz et al. 2022

### **10 Points**

- 1. No generalization to the full international variance in systems
- 2. NEPS: case numbers too small and biased distributions
- 3. Wrong operationalization of class composition (,,leave-i-out")
- 4. Wrong and misleading mediation-analyses
- 5. Interaction of cognitive niveau and homogeneity
- 6. Control of school-types
- 7. Abilities and achievements as equivalents
- 8. No control of achievements before
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The crucial quote



#### **Theoretical Background**

**MoAbiT** (Causal Model)

... simplified (secondary school only)







### **Control for ACE?**








Relations of input, ability, efficiency of learning and achievement as output

General learning function

Backgroun

Conditions and Efficiency of Learning

> Learning as **TOTAL** result of **conditions** and **efficiency**

















# ... and THIS was (therefore) OUR estimand/replicandum!

erklärende Bedingung für die **Cognitive abilities** are specifically used as Als Leistungen in der Sekundarstufe werden explanatory condition for achievement in kognitiven Fähigkeiten secondary school, both individually and as a gezielt die verwendet, individuell wie als Kontext- contextual feature, and **not** the achievement Merkmal, und nicht die Leistungen vorher beforehand in elementary school. For this is in der Grundschule. Denn darum geht es in what the theoretical arguments for den Begründungen für die Differenzierung: differentiation are about: that latent Dass sich damit die latenten kognitiven cognitive abilities can unfold, also entfalten können, auch **independently** of what has been shown up Fähigkeiten unabhängig davon, was bis dahin und to then and currently in terms of aktuell an Leistungen gezeigt worden ist. achievement. (ES 2020: 190) (ES 2020: 190)

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**Empirical Comparisons** 

#### 1. Mediation

(unconditional T-Effect)

#### Analyses ES 2020

		MoAt	biT	1	2	3	4	5	6
SES: Socioeconomic background	SES	+			0.67	0.42	0.40	0.40	0.40
NSES: Level SES school class (mean) HSES: Homogeneity SES school class (sd <sup>-1</sup> ) Interaction NSES and HSES	NSES HSES NSES*HSES	SHI	IFT	from SSI	ES to	6.73 2.32 -4.96	4.56 1.42 -3.06	<b>2.39</b> 0.58 -1.48	1.14 0.26 -0.73
ACE: Prior achievement ABL: General cognitive abilities	ACE ABL	+	_	SABL			*** 1.59	*** 1 43	*** 1.43
NABL: Level ABL school class (mean) HABL: ABL school class (sd <sup>-1</sup> ) Interaction NABL and HABL	NABL HABL NABL*HABL	+ + +		"co repl	orrecting lication"	:		<b>2.19</b> <b>1.01</b> -1.58	<b>1.46</b> 0.75 -1.22
GYM: School Type	GYM	+							0.51
T: Stringency Differentiaton	T(3)	≥0	)	0.29	0.26	0.14	0.15	0.14	0.14
	T-Effect (unconditiona	al)						positive rema	T-Effect ins!

		MoAbiT	1	2	3	4	5	6
SES: Socioeconomic background	SES	+					0.40	
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GYM: School Type	GYM	+						
T: Stringency Differentiaton	T(3)	≥0					0.14	

### "Replication" NN 2022

		MoAbiT	1	2	3	4	ES2020	6
SES: Socioeconomic background	SES	+					0.40	
NSES: Level SES school class (mean) HSES: Homogeneity SES school class (sd <sup>-1</sup> ) Interaction NSES and HSES	NSES HSES NSES*HSES	+ + 0					<b>2.39</b> 0.58 -1.48	
ACE: Prior achievement ABL: General cognitive abilities	ACE ABL	*** +					*** 1.43	
NABL: Level ABL school class (mean) HABL: ABL school class (sd <sup>-1</sup> ) Interaction NABL and HABL	NABL HABL NABL*HABL	+ + +					<b>2.19</b> <b>1.01</b> -1.58	
GYM: School Type	GYM	+						
T: Stringency Differentiaton	T(3)	≥0					0.14	

		MoAbiT	1	2	3	4	ES2020	NN2022
SES: Socioeconomic background	SES	+					0.40	0.06
NSES: Level SES school class (mean) HSES: Homogeneity SES school class (sd <sup>-1</sup> ) Interaction NSES and HSES	NSES HSES NSES*HSES	+ + 0					<b>2.39</b> 0.58 -1.48	0.95 0.26 -0.63
ACE: Prior achievement ABL: General cognitive abilities	ACE U ABL di	ncondit sappea	ional T <b>rs</b> with	-Effect control			*** 1.43	0.55 0.13
NABL: Level ABL school class (mean) HABL: ABL school class (sd <sup>-1</sup> ) Interaction NABL and HABL GYM: School Type	NABL HABL NABL*HABL GYM	of + + +	ACE OVE	RCON	FROL!		<b>2.19</b> <b>1.01</b> 1.58	<b>1.05</b> 0.63 -0.78
T: Stringency Differentiaton	T(3)	≥0	ł	out even nega	then <b>: N</b> tive!	ΟΤ	0.14	0.05

**2.** Moderation

(conditional HABL-Effect)

Constructs	ES 2022 without ACE	ES 2022 with ACE
T(3)	-1.22	-1.20
SES	х	х
T*SES	х	х
T*NSES	X	X
T*HSES	х	х
T*NSES*HSES	X	Х
ACE	***	Х
ABL	X	Х
T*ABL	-0.14	-0.12
T*NABL	3.18	2.27
T*HABL	2.49	1.82
T*NABL*HABL	-4.14	-3.04

Constructs	ES 2022 without	ES 2022 with
<b>T</b> (2)	ACE	ACE
1(3)	-1.22	-1.20
SES	X	Х
T*SES	Х	X
T*NSES	Х	X
T*HSES	Х	X
T*NSES*HSES	X	Х
	ste ste ste	
ACE	***	X
ABL	Х	Х
T*ABL	-0.14	-0.12
T*NABL	3.18	2.27
T*HABL	2.49	1.82
T*NABL*HABL	-4.14	-3.04

	Constructs T(3)	<b>ES 2022</b> <b>without</b> <b>ACE</b> -1.22	<b>ES 2022</b> <b>with</b> <b>ACE</b> -1.20	Analyses <b>controlling</b> for baseline performance in grade 5
	SES	х	х	yiel <u>ded comparable</u> findings.
	T*SES	X	X	(ES 2020: 290)
	T*NSES T*HSES	X X	X X	
	T*NSES*HSES	X	X	
	ACE ABL	*** X	X X	Effect of homogenization REMAINS!
	T*ABL	-0 14	-0.12	
Three-way!	T*NABL T*HABL T*NABL*HABL	3.18 2.49 -4.14	2.27 1.82 -3.04	effects disappears in NN only,
				because the <b>empirical</b> estimand

was changed: from three-way to two-way

### **Three**way-Interaction

Strictness of ABL-Tracking Level of ABL in schoolclass Homogeneity of ABL in schoolclass

#### T\*NABL\*NABL

Graphical illustration

theoretical foundation:

Ability-Treatment Interaction (ATI)

#### **Effects of T\*NABL\*HABL**



... the critiques and replications of NN and others were a great step in a further clarifying this longstandig dispute

... even if they were largely wrong, Estimands a distorting and at least partly ignorant The Dispute of what could be found in the originals.

Theory **Re-Corrections Conclusions** 

... and don't forget what was before:







#### Addenda
# **1. Threeway- Interaction**

# **Three**way-Interaction

Strictness of ABL-Tracking Level of ABL in schoolclass Homogeneity of ABL in schoolclass

#### T\*NABL\*NABL

Graphical illustration

theoretical foundation:

Ability-Treatment Interaction (ATI)

#### **Effects of T\*NABL\*HABL**



2. The Standard-Position A Reminder













**3. Ability- or Achievement-Tracking?** 

Ability-Tracking	Achievement-Tracking
0.19	0.01
-0.99	
A	CH is NOT the same
-0.02	
-0.54	0.21
-0.56	-0.05
0.51	0.64
-0.14	-0.07
2.93	-0.18
2.46	0.24
-4.09	-0.13
0.22	0.30
-2.23	<b>Explains why all these</b>
0.14	substitues don't work!
0.88	Substitues uon t work.
2636	2636
313	313
	Ability-Tracking 0.19 -0.99 -0.02 -0.54 -0.56 0.51 -0.14 2.93 2.46 -4.09 0.22 -2.23 0.14 0.88 2636 313

## **4.** The Other Points

### **10 Points**

- 1. No generalization to the full international variance in systems
- 2. NEPS: case numbers too small and biased distributions
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### **10 Points**

#### ... but conditional on **implementation** of Ability-Tracking!

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NEPS: case numbers too small and biased distributions

### **10 Points**

... small, indeed, but **not** biased!

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Wrong operationalization of class composition (,,leave-iout")

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**wrong** application of ,,leave-iout"-rule for the **given** case

ACS as dependent variable, but **ABL** as contextual variable

"leave-i-out" applies only for peer-effects, but **no**t for curriculum/instruction



10. Two-way- instead of three-way-interactions

... **change** of general effects and moderation

**Systemeffects** 

### **10 Points**

... two-way-interaction of NABL\*NABL superfluos and misleading

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... **no** way! (Aptitude-treatmentinteraction)

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... GYM not considered

... arbitrary omission of a central aspect of any differentiated system (cf. Domina et al. 2019)

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NO! (see above)

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See the scheme of MoAbit

#### general Relations (all systems)







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... **ignorance** of the theoretical foundation (ATI) and arbitrary **distortion** of the decisive empirical estimand

Threeway-interaction (T\*NABL\*HABL) ,,overly complex", therefore only the two two-way-interactions (T\*NABL, T\*HABL)

T\*HABL-effect disappears!